# Energy of Chemical Bonds and Spatial Energy Principles of the Hybridization of Atom Orbitals 

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#### Abstract

Methods for the evaluation of energy directedness of atom orbital hybridization and the calculation of the energy of chemical bonds in simple and complex structures are proposed on the basis of the application of the spatial energy parameter concept. Appropriate calculations and comparisons for 68 compounds were made. The calcu-


lation results agreed with the experimental data. © 2006 Wiley
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Key words: spatial-energy parameter; hybridization; bond energy

## INTRODUCTION

Bond energy is a direct measure of chemical bond strength. Its value is determined by the work necessary to destroy the bond between the atoms of a molecular structure (or the gain of energy in the formation process of this structure from atoms). If the molecule contains two or more similar bonds, the breakoff energy of this bond differs from its average energy (by all bonds).

The values of the bond energy of the electrons of free atoms are calculated by quantum-mechanical methods via the wave functions. ${ }^{1}$ However, their practical application for the determination of the energy values of interatomic bonds of actual structures produces significant difficulties because the values of electron bond energy in these structures depend on the changes in the electron and nucleus configuration of the systems, especially during the hybridization of atom orbitals. The prognostic evaluation of such processes is still not properly developed.

Therefore, the main computational method for determining the values of chemical bond energy is the use of corresponding thermochemical values (enthalpies of the formation of reaction products and the initial molecule).

It is of interest in both the theoretical and practical senses to arrange a more direct dependence between

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the character of changes in the initial energy characteristics of an atom and the value of its chemical bond energy.

In this respect, it is important to experimentally study the electron spectra of different (not only molecular) structures by means of X-ray electron spectroscopy, which allows one to estimate the electron bond energies in complex systems. ${ }^{2}$

In this research, we attempted to estimate the energy of chemical bonds on the basis of the initial spatial energy characteristics of free atoms with the help of the concept of the spatial energy parameter $(P)$, taking into consideration their changes during the hybridization of atom orbitals.

## Method substantiation

The analysis of various physicochemical macroprocesses and microprocesses results in the conclusion that, in many cases, the inverse values of kinetic or energy parameters of subsystems are added when the resulting interaction of atom-molecular structures is estimated. Therefore, the tabulated (initial) values of Ps can be calculated on the basis of the principle of the addition of inverse values of energy components of free atom systems: ${ }^{3}$

$$
\begin{gather*}
\frac{1}{P_{0}}=\frac{1}{q^{2}}+\frac{1}{(w r n)_{i}}  \tag{1}\\
P_{E}=\frac{\sum P_{0}}{R} \tag{2}
\end{gather*}
$$

TABLE I
P Parameters of Atoms Calculated via the Bond Energy of the Electrons


TABLE I Continued

| $\begin{gathered} \text { Atom } \\ \text { I } \end{gathered}$ | Valence electrons 2 | $\begin{gathered} w \\ (\mathrm{eV}) \\ 3 \end{gathered}$ | $r_{i}(\AA)$ 4 |  |  | $R(\AA)$ 7 | $\begin{gathered} \hline P_{0} / R \\ (\mathrm{cV}) \\ 8 \end{gathered}$ | к 9 | $P_{E} / \kappa$ 10 | $\begin{gathered} r_{1} \\ (\AA) \\ 11 \end{gathered}$ | $\begin{gathered} P_{0} / r_{1} \\ (\mathrm{eV}) \\ 12 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sn | $5 p^{1}$ | 7.2124 | 1.240 | 47.714 | 7.5313 | 1.42 | 5.3037 |  |  |  |  |
|  |  |  |  |  |  | 1.58 | 4.7666 |  |  |  |  |
|  | $5 p^{2}$ |  |  |  | 13.0091 | 1.42 | 9.1613 |  |  | 1.02 | 12.754 |
|  |  |  |  |  |  | 1.58 | 8.2336 |  |  |  |  |
|  | $\begin{aligned} & 5 p^{3}{ }_{r} \\ & 5 s^{1} \end{aligned}$ | 12.965 | 1.027 | 65.062 | 17.173 | 1.42 | 12.094 |  |  |  |  |
|  |  |  |  |  | 11.053 | 1.42 | 7.7838 |  |  |  |  |
|  |  |  |  |  |  | 1.58 | 6.9956 |  |  |  |  |
|  | $5 s^{2}$ |  |  |  | 18.896 | 1.42 | 13.307 |  |  |  |  |
|  |  |  |  |  |  | 1.58 | 11.959 |  |  |  |  |
|  | $5 p^{2}+5 s^{2}$ |  |  |  | 26.427 | 1.42 | 18.611 |  | 0.67 |  | 38.443 |
|  |  |  |  |  |  | 1.58 | 16.726 |  | 0.67 |  |  |
| Cl | $3 \mathrm{p}^{1}$ | 13.780 | 0.7235 | 59.844 | 8.5461 | 1.00 | 8.5461 |  | 1.81 | 4.7216 |  |
|  | $3 \mathrm{p}^{3}$ |  |  |  | 19.943 |  |  |  |  |  |  |
|  | $3 p^{5}$ | 13.780 | 0.7235 | 59.844 | 27.196 | 1.00 | 27.196 |  |  |  |  |
|  | $3 \mathrm{~s}^{1}$ | 29.196 | 0.660 | 79.928 | 15.526 | 1.00 | 15.526 |  |  |  |  |
|  | $3 s^{2}$ | 29.196 | 0.660 | 79.928 | 26.002 |  |  |  |  |  |  |
|  | $3 \mathrm{~s}^{1}+3 \mathrm{p}^{3}$ |  |  |  | 35.468 | 1.00 | 35.468 | 4 | 8.867 |  |  |
|  | $3 s^{2}+3 p^{5}$ |  |  |  | 53.198 | 1.00 | 53.198 |  | 1.81 | 29.391 |  |
| Br | $4 \mathrm{p}^{1}$ | 12.438 | 0.8425 | 73.346 | 9.1690 | 1.14 | 8.0430 |  | 1.96 | 4.6781 |  |
|  | $4 p^{3}$ |  |  |  | 22.005 | 1.14 |  |  |  |  |  |
|  | $4 p^{5}$ |  |  |  | 30.563 |  | 26.809 |  |  |  |  |
|  | $4 \mathrm{~s}^{1}$ | 27.013 | 0.730 | 100.21 | 16.477 |  | 14.454 |  |  |  |  |
|  | $4 \mathrm{~s}^{2}$ |  |  |  | 28.300 |  | 24.825 |  |  |  |  |
|  | $4 \mathrm{~s}^{1}+4 \mathrm{p}^{3}$ |  |  |  | 38.462 | 1.14 | 33.739 | 4 | 8.4348 |  |  |
|  | $4 \mathrm{~s}^{2}+4 \mathrm{p}^{5}$ |  |  |  | 58.863 |  | 51.634 |  | (0.39) | 150.93 |  |
| I | $5 p^{1}$ | 10.971 | 1.0215 | 77.651 | 9.7936 | 1.35 | 7.2545 |  | 2.20 | 4.4516 |  |
|  | $5 p^{3}$ |  |  |  | 23.462 | 1.35 | 13.739 | 3 | 4.580 |  |  |
|  | $5 p^{5}$ |  |  |  | 32.548 |  | 24.109 |  |  |  |  |
|  | $5 \mathrm{~s}^{1}$ | 22.345 | 0.876 | 103.44 | 16.459 |  | 12.192 |  |  |  |  |
|  | $5 \mathrm{~s}^{2}$ |  |  |  | 28.400 |  | 21.037 |  |  |  |  |
|  | $5 s^{2}+5 p^{5}$ |  |  |  | 60.948 |  | 45.147 |  | 0.50 | 121.90 |  |

where $w_{i}$ is the bond energy of electrons; ${ }^{1} r_{i}$ is the orbital radius of the $i$ orbital; $^{4} n_{i}$ is the number of electrons in the given orbital; $q=Z^{*} / n^{*}$, where $Z^{*}$ and $n^{*}$ are the nucleus effective charge and effective main quantum number, respectively; ${ }^{5,6}$ and $R$ is the dimensional characteristics of the atom bond.

Values of tabulated atomic P-parameter $\left(P_{0}\right)$ are constant for electrons of the $i$ orbital of the given atom.

As described in ref. 3, $P_{E}$ is a parameter that numerically equals the energy of the valence electrons in an atom static model, which is a direct characteristic of electron density inside the atom at a given distance from the nucleus and, therefore, can be used to estimate the kinetics of chemical reactions and chemical bond energy of structures.
$P_{0}$ and $P_{E}$ of free atoms were calculated with eqs. (1) and (2), the results of which are given in Table I. For the hydrogen atom, the value of the Bohr radius of the hydrogen atom was equal to $0.529 \AA$; for some cases, the ionic radius ( $r_{I}=1.36 \AA$ ) was used as the main dimensional characteristic.

All atoms, covalent radii, and $r_{I}$ values were taken basically according to Belov-Bokii. For C, N, and O atoms, the possibility of changing covalent radii, de-
pending on the bond repetition factor, was also taken into consideration. For the same elements, the average statistical values of $P$ were given as $P_{E} / K$, which assumed the possibility for further calculation of the average value of bond energy.

## Spatial energy principles of hybridization

Hybridization refers to the mixing of atom orbitals of different types of a given atom in one molecular (or atom) orbital. Hybridization principles are well-developed in accordance with the experimental data in the frames of general theories of valence bonding and molecular orbitals.

However, the sources of energy directedness of hybridization processes have to be further investigated and discussed.

The authors of ref. 1 made a conclusion based on the analysis of multiple computational and experimental data in which the most valence-active were the orbitals with minimum values of $P_{0}$. We applied this principle to the hybridization of atom orbitals to the example of carbon and nitrogen atoms.

TABLE II

## Computation of Bond Energy Taking into Account the Hybridization of Atom Orbitals

| Structure$1$ | $\begin{gathered} \text { Bond } \\ 2 \end{gathered}$ | Hybridization 3 | Orbitals | $\begin{gathered} P_{o^{\prime}} \\ (\mathrm{eVA}) \\ 5 \end{gathered}$ | $\begin{gathered} \sum P_{0^{\prime}}{ }^{2} \\ (\mathrm{eVA}) \\ 6 \end{gathered}$ | $R \underset{\substack{R_{k} \\(A) \\(A) \\ 7}}{ }$ | $\begin{gathered} P_{E}^{\prime} \\ (\mathrm{eV}) \\ 8 \end{gathered}$ | $\begin{gathered} (N / \kappa)_{1} \\ 9 \end{gathered}$ | $\begin{gathered} P_{E}^{\prime \prime}(\mathrm{eV}) \\ 10 \end{gathered}$ | $\begin{gathered} (N / \kappa)_{2} \\ 11 \end{gathered}$ | $P_{C}$ $(\mathrm{eV})$ <br> 12 | $E\left(\frac{\mathrm{~kJ}}{\mathrm{~mol}}\right)$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  | $\begin{gathered} \text { Calcd } \\ 13 \end{gathered}$ | Found 14 |
| Diamond | $\sigma$ | $\mathrm{sp}^{3}$ | $2 \mathrm{~s}^{1}$ | 9.0209 | 22.234 | 0.772 | 28.801 | 1/4 | 28.801 | 1/4 | 3.600 | 347.5 | 347.3 |
|  | $\mathrm{C}-\mathrm{C}$ |  | $2 \mathrm{p}_{\mathrm{r}}{ }^{3}$ | 13.213 |  |  |  |  |  |  |  |  |  |
| Graphite (1) | $\sigma$ | $\mathrm{sp}^{2}$ | $2 \mathrm{~s}^{1}$ | 9.0209 | 19.082 | 0.710 | 26.876 | 1/3 | 26.876 | 1/3 | 4.479 | 432.4 | 418.7-460.6 |
|  | $\mathrm{C}-\mathrm{C}$ |  | $2 \mathrm{p}^{2}$ | 10.061 |  |  |  |  |  |  |  |  |  |
| Graphite (2) | $\sigma$ | $\mathrm{s}^{2} \mathrm{p}^{2}$ | $2 \mathrm{~s}^{2}$ | 14.524 | 24.585 | 0.710 | 34.627 | 1/4 | 34.627 | 1/4 | 4.3283 | 417.8 | 418.7 |
|  | C-C |  | $2 \mathrm{p}^{2}$ | 10.061 |  |  |  |  |  |  |  |  |  |
| Carbyne$(-\mathrm{C} \equiv \mathrm{C}-)_{1}$ | Single | sp | $2 \mathrm{~s}^{1}$ | 9.0209 | 13.425* | 0.6895 | 9.7365 | 1/4 | 9.7365 | 1/4 | 1.2170 | 117.5 | 108.9 |
|  |  |  | $2 \mathrm{p}_{\mathrm{r}}{ }^{1}$ | 4.4044 | *1/2 |  |  |  |  |  |  |  |  |
| Ethylene <br> $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}$ <br> Acetylene <br> $\mathrm{HC} \equiv \mathrm{CH}$ | $\sigma$ | $\mathrm{sp}^{2}$ | $2 \mathrm{~s}^{1}$ | 9.0209 | 19.082 | 0.665 | 28.695 | 2/4 | 28.695 | 2/4 | 3.587 | 346.2 | 347 |
|  | C-C |  | $2 \mathrm{p}^{2}$ | 10.061 |  |  |  |  |  |  |  |  |  |
|  | $\sigma$ | sp | $2 \mathrm{~s}^{1}$ | 9.0209 | 13.425 | 0.601 | 22.375 | 3/4 | 22.375 | 3/4 | 8.391 | 807.6 | 782 |
|  | C-C |  | $2 \mathrm{p}^{1}{ }_{\text {t }}$ | 4.4044 |  |  |  |  |  |  |  |  |  |
|  | $\pi$ |  | $2 \mathrm{~s}^{1}$ | 4.4044 | 8.8088 | 0.601 | 14.657 | 1/4 | 14.657 | 1/4 | 1.832 | 176.8 |  |
|  | $\mathrm{C}-\mathrm{C}$ |  | $2 p_{\mathrm{r}}{ }^{1}$ | 4.4044 |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { Methane (1) } \\ & \mathrm{CH}_{4} \end{aligned}$ | $\sigma+\pi$ |  |  |  |  |  |  |  |  |  |  | 984.4 | 962.3 |
|  | $\sigma$ | sp ${ }^{3}$ | $2 \mathrm{~s}^{1}$ | 9.0209 | 22.234 | 0.546 | 40.722 | 1/4 | 4.7985 | 1/1 | 4.716 | 455.3 | 435.1 |
|  |  |  |  |  |  |  |  |  | 0.546 |  |  |  |  |
|  | C-H |  | $2 \mathrm{p}_{\mathrm{r}}{ }^{3}$ | 13.213 |  |  |  |  |  |  |  |  |  |
| Methane (2) | $\mathrm{C}-\mathrm{H}$ |  | $2 \mathrm{~s}^{2}$ | 14.524 | 24.585 | 0.77 | 31.929 | 1/4 | 9.0624 | 1/1 | 4.243 | 409.6 | 410 |
|  |  |  | $2 \mathrm{p}^{2}$ | 10.061 |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { Ethane } \\ & \mathrm{H}_{3} \mathrm{C}-\mathrm{CH}_{3} \end{aligned}$ | $\sigma$ | $\mathrm{sp}^{3}$ | $2 \mathrm{~s}^{1}$ | 9.0209 | 22.234 | 0.772 | 28.819 | 1/4 | 28.819 | 1/4 | 3.6024 | 347.7 | 345.6 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | C-C |  | $2 \mathrm{p}_{\mathrm{r}}{ }^{3}$ | 13.213 |  |  |  |  |  |  |  |  |  |
| Nitrogen $\mathrm{N}_{2}$ | $\mathrm{N}-\mathrm{N}$ | - | $2 p^{1}$ | 6.5916 | 13.183 | 0.71 | 18.658 | $1 / 3$ | 18.658 | 1/3 | 3.095 | 298.7 | 318 |
|  |  |  | $2 \mathrm{p}^{1}$ | 6.5916 |  |  |  |  |  |  |  |  |  |
|  | $\mathrm{N}=\mathrm{N}$ | - | $2 \mathrm{p}^{2}$ | 11.723 | 23.446 | 0.63 | 37.216 | 1/3 | 37.216 | 1/3 | 6.2026 | 598.7 | 586 |
|  |  |  | $2 \mathrm{p}^{2}$ | 11.723 |  |  |  |  |  |  |  |  |  |
| $\mathrm{N}_{2} \mathrm{~N} \equiv \mathrm{~N}$ | $\sigma$ | sp | $2 \mathrm{p}_{\mathrm{r}}{ }^{4}$ | 19.193 | 19.193 | 0.55 | 34.896 | 1/3 | 34.896 | 1/3 | 5.8161 | 561.4 | 543.4 |
|  | $\mathrm{N}-\mathrm{N}$ |  |  |  |  |  |  |  |  |  |  |  |  |
|  | $2 \pi$ |  | $2 p_{r}{ }^{5}$ | 21.966 | 21.966 | 0.55 | 39.938 | 1/5 | 39.938 | 1/5 | 3.9938 | 385.5 |  |
|  | $\mathrm{N}-\mathrm{N}$ |  |  |  |  |  |  |  |  |  |  |  |  |
|  | $\mathrm{N}-\mathrm{N}$ |  |  |  |  |  |  |  |  |  |  |  |  |
|  | $\sigma+\pi$ |  |  |  |  |  |  |  |  |  |  | 946.9 | 947.6 |
| $\begin{aligned} & \text { Silicon } \\ & \mathrm{Si}_{2} \rightarrow 2 \mathrm{Si} \end{aligned}$ | $\mathrm{Si}-\mathrm{Si}$ | $\mathrm{s}^{2} \mathrm{p}^{2}$ | $3 s^{2}$ | 15.711 | 26.587 | 1.11 | 23.952 | 1/4 | 23.952 | 1/4 | 2.994 | 289 | $305 \pm 3$ |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | $\sigma$ |  | $3 \mathrm{p}^{2}$ | 10.876 |  |  |  |  |  |  |  |  | $309.6 \pm 13$ |
|  |  |  | $3 \mathrm{p}_{\mathrm{r}}{ }^{3}$ | 13.766 | 13.766 | 1.34 | 10.273 | 1/3 | 10.273 | 1/3 | 1.712 | 165.3 | 176 |
| $\mathrm{SiH}_{4}$ | $\mathrm{Si}-\mathrm{H}$ | $\mathrm{sp}^{3}$ | $3 \mathrm{~s}^{1}$ | 9.8716 | 23.638 | 0.738 | 32.030 | 1/4 | 9.0624 | 1/1 | 4.251 | 410.3 | 395 |
|  |  |  | $3 \mathrm{p}_{\mathrm{r}}{ }^{3}$ | 13.766 |  |  |  |  |  |  |  |  |  |
| $\begin{array}{r} \text { Germanium } \\ \mathrm{Ge}_{2} \rightarrow 2 \mathrm{Ge} \end{array}$ | $\mathrm{Ge}-\mathrm{Ge}$ | $\mathrm{sp}^{3}$ | $4 \mathrm{~s}^{1}$ | 10.855 | 26.658 | 1.22 | 21.851 | 1/4 | 21.851 | 1/4 | 2.7314 | 263.6 | 273 |
|  | $\sigma$ |  | $4 \mathrm{p}_{\mathrm{r}}{ }^{3}$ | 15.803 |  |  |  |  |  |  |  |  | $278 \pm 13$ |
|  |  |  | $4 \mathrm{p}_{\mathrm{r}}{ }^{3}$ | 15.803 | 15.803 | 1.39 | 11.369 | 1/3 | 11.369 | 1/3 | 1.895 | 183 | 168 |
| $\operatorname{Tin}_{\mathrm{Sn}_{2} \rightarrow 2 \mathrm{Sn}}$ | $\mathrm{Sn}-\mathrm{Sn}$ | $5 \mathrm{p}_{\mathrm{r}}{ }^{3}$ | $5 p_{r}{ }^{3}$ | 17.173 | 17.173 | 1.42 | 12.094 | 1/3 | 12.094 | 1/3 | 2.016 | 194.6 | $192.5 \pm 16.7$ |
| Sn (II) | $\mathrm{Sn}-\mathrm{Sn}$ | $\mathrm{p}^{2}$ | $5 p^{2}$ | 13.009 | 13.009 | 1.63 | 7.981 | 1/2 | 7.981 | 1/2 | 1.995 | 192.6 | 192.5 |
| Sn(IV) | $\mathrm{Sn}-\mathrm{Sn}$ | $\mathrm{s}^{2} \mathrm{p}^{2}$ | $5 p^{2}$ | 13.009 | 26.427 | 1.58 | 16.726 | 1/4 | 16.726 | 1/4 | 2.098 | 202.5 | 192.5 |
|  |  |  | $5 \mathrm{~s}^{2}$ | 18.896 |  |  |  |  |  |  |  |  |  |
| HF | $\sigma$ | $\mathrm{sp}^{2}$ | $2 \mathrm{~s}^{1}$ | 14.375 | 31.808 | 0.64 | 49.700 | 1/4 | 4.79851/0.438 | 1/1 | 5.822 | 562 | 566 |
|  | F-H |  | $2 p^{3}$ | 17.433 |  |  |  |  | 0.438 |  |  |  |  |
| HCl | $\sigma$ | $\mathrm{sp}^{2}$ | $3 \mathrm{~s}^{1}$ | 15.526 | 35.468 | 1.00 | 35.468 | 1/4 | 4.7985/0.529 | 1/1 | 4.482 | 432.6 | 427.8 |
|  | $\mathrm{Cl}-\mathrm{H}$ |  | $3 p^{2}$ | 19.943 |  |  |  |  | 0.529 |  |  |  |  |
| HBr | $\sigma$ | $\mathrm{sp}^{2}$ | $4 \mathrm{~s}^{1}$ | 16.477 | 38.462 | 1.14 | 33.734 | 1/4 | 4.7985/0.704 | 1/1 | 3.769 | 363.9 | 362.5 |
|  | $\mathrm{Br}-\mathrm{H}$ |  | $4 p^{3}$ | 22.005 |  |  |  |  | 0.704 |  |  |  |  |
| HI | I-H | $\mathrm{p}^{3}$ | $5 p^{3}$ | 23.462 | 23.462 | 1.35 | 17.379 | 1/3 | 4.7985/0.8045 | 1/1 | 2.94 | 283.7 | 294.6 |

$P_{0}{ }^{\prime}$, tabulated atomic P-parameter of the given atom; $R_{K}$, cation radius; $d$, bond length.

## Carbon $\left(2 s^{2} 2 p^{2}\right)$

As shown in Table I, the maximum value of $P_{0}$ of the $2 \mathrm{p}^{2}$ orbital was $10.061 \mathrm{eV} \AA$, but the minimum value of $P_{0}$ of the $2 s^{1}$ orbital was smaller ( $9.029 \mathrm{eV} \AA$ ). This means that the $2 s^{1}$ orbital was more valence-active than the $2 \mathrm{p}^{2}$
orbital. This conditioned their hybridization. The calculation, according to eq. (1), produced a value of $P_{0}$ of the $2 p^{3}$ (hybridized) orbital equal to $13.213 \mathrm{eV} \AA$. This was much smaller than $P_{0}$ of the $2 \mathrm{~s}^{2}$ orbital ( $14.524 \mathrm{eV} \AA$ ). Therefore, only the following hybridization options

TABLE III
$D_{0}(\mathrm{~kJ} / \mathrm{mol})$ Values of the Diatomic Molecules

| Structure | First atom |  |  |  | Second atom |  |  |  | $\begin{gathered} P_{C} \\ (\mathrm{eV}) \end{gathered}$ | $\mathrm{D}_{0}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Orbitals | $N / \kappa$ | $P_{E}(\mathrm{eV})$ | $P_{E} \frac{N}{\kappa}$ | Orbitals | N/к | $\begin{gathered} P_{E} \\ (\mathrm{eV}) \end{gathered}$ | $P_{E} \frac{N}{\kappa}$ |  | Calcd | Found |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| CCl | $2 p^{1}$ | 1/1 | 7.6208 | 7.6208 | $3 p^{1}$ | 1/1 | 8.5461 | 8.5461 | 4.0209 | 388.9 | 393.3 |
| CBr | $2 p^{1}$ | $1 / 1$ | 7.6208 | 7.6208 | $4 p^{1}$ | 1/1 | 8.0430 | 8.0430 | 3.9130 | 377.7 | 364 |
| CJ | $2 \mathrm{p}^{1}$ | 1/1 | 7.6208 | 7.6208 | $5 p^{1}$ | 1/1 | 7.2545 | 7.2545 | 2.2523 | 217.4 | 209.2 |
| CN | $2 \mathrm{p}^{2}$ | 2/2 | 13.066 | 13.066 | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{3}$ | 2/5 | 47.413 | 18.965 | 7.7358 | 746.7 | 755.6 |
| CN | $2 \mathrm{p}^{2}$ | 2/2 | 14.581 | 14.581 | $2 p^{3}$ | 2/3 | 25.127 | 16.751 | 7.796 | 752.5 | 755.6 |
| $\mathrm{C}-\mathrm{O}$ | $2 \mathrm{p}^{2}$ | 1/2 | 13.066 | 6.533 | $2 \mathrm{p}^{2}$ | 1/2 | 17.967 | 8.984 | 3.782 | 365 | 356 |
| NO | $2 p^{1}$ | 1/1 | 9.2839 | 9.2839 | $2 p^{2}$ | 2/2 | 20.048 | 20.048 | 6.346 | 612.5 | 626.8 |
| CH | $2 \mathrm{p}^{2}$ | 1/2 | 13.066 | 6.533 | $1 \mathrm{~s}^{1}$ | 1/1 | 9.066 | 9.066 | 3.7969 | 366.5 | $333 \pm 1$ |
| OH | $2 \mathrm{p}^{2}$ | $1 / 2$ | 17.967 | 8.9835 | $1 \mathrm{~s}^{1}$ | 1/1 | 9.066 | 9.066 | 4.5118 | 435.5 | 423.7 |
| CIF | $3 \mathrm{~s}^{2} 3 \mathrm{p}^{5}$ | $1 / 7$ | $29.391^{\text {a }}$ | 4.1987 | $2 s^{2} 2 p^{5}$ | 1/7 | $38.202^{\text {a }}$ | 5.4574 | 2.5579 | 246.9 | 229.1 |
| CIO | $3 s^{2} 3 p^{5}$ | $1 / 7$ | $29.391^{\text {a }}$ | 4.1987 | $2 \mathrm{p}^{2}$ | 2/2 | $8.7191^{\text {a }}$ | 8.7191 | 2.8337 | 273.5 | 264 |
| CIO | $3 \mathrm{p}^{1}$ | $1 / 1$ | $4.7216^{\text {a }}$ | 4.7216 | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{4}$ | 1/6 | $30.738^{\text {a }}$ | 5.123 | 2.450 | 237.2 | 264 |
| FO | $2 p^{1}$ | 1/1 | $4.9887^{\text {a }}$ | 4.9887 | $2 p^{2}$ | 1/2 | $8.7191^{\text {a }}$ | 4.3596 | 2.327 | 224.6 | 219.2 |
| NF | $2 \mathrm{p}^{3}$ | 1/3 | $10.696^{\text {a }}$ | 3.5653 | $2 p^{1}$ | 1/7 | $38.202^{\text {a }}$ | 5.4574 | 2.486 | 239.5 | 298.9 |
| NCL | $2 p^{3}$ | 1/3 | 22.296 | 7.432 | $3 \mathrm{p}^{1}$ | 1/1 | 8.5461 | 8.5461 | 3.9751 | 383.7 | 384.9 |
| $\mathrm{H}_{2}$ | $1 \mathrm{~s}^{1}$ | $1 / 1$ | 9.0624 | 9.0624 | $1 \mathrm{~s}^{1}$ | 1/1 | 9.066 | 9.066 | 4.533 | 437.5 | 432.2 |
| $\mathrm{Li}_{2}$ | $2 \mathrm{~s}^{1}$ | $1 / 1$ | 2.2419 | 2.2419 | $2 \mathrm{~s}^{1}$ | 1/1 | 2.2419 | 2.2419 | 1.121 | 108.2 | 98.99 |
| $\mathrm{B}_{2}$ | $2 p^{1}$ | $1 / 1$ | 5.4885 | 5.4885 | $2 p^{1}$ | 1/1 | 5.4885 | 5.4885 | 2.744 | 264.9 | $276 \pm 21$ |
| $\mathrm{C}-\mathrm{C}$ | $2 p^{1}$ | 1/1 | 7.6208 | 7.6208 | $2 p^{1}$ | 1/1 | 7.6208 | 7.6208 | 3.810 | 367.8 | 376.7 |
| $\mathrm{C}=\mathrm{C}$ | $2 \mathrm{p}^{1}$ | 2/2 | 13.066 | 13.066 | $2 \mathrm{p}^{2}$ | 2/2 | 13.066 | 13.066 | 6.533 | 630.6 | 611 |
| $\mathrm{N}-\mathrm{N}$ | $2 \mathrm{p}^{3}$ | 1/3 | $10.696^{\text {a }}$ | 3.5653 | $2 \mathrm{p}^{3}$ | 1/3 | $10.696^{\text {a }}$ | 3.5653 | 1.783 | 172.1 | 161 |
| $\mathrm{N}=\mathrm{N}$ | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{3}$ | 2/5 | $22.745^{\text {a }}$ | 9.098 | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{3}$ | 2/5 | $22.745^{\text {a }}$ | 9.098 | 4.549 | 439 | 418 |
| $\mathrm{O}-\mathrm{O}$ | $2 \mathrm{p}^{2}$ | 1/2 | 8.7191 | 4.3596 | $2 \mathrm{p}^{2}$ | 1/2 | 8.7191 | 4.3596 | 2.1798 | 210.4 | 213.4 |
| $\mathrm{O}=\mathrm{O}$ | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{4}$ | 2/6 | $30.738^{\text {a }}$ | 10.246 | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{4}$ | 2/6 | $30.738^{\text {a }}$ | 10.246 | 5.123 | 494.5 | 498.3 |

${ }^{\text {a }}$ Calculations of $P_{E}$ are given with $r_{1}$ based on the equation $P_{E}=\Sigma P_{0} / r_{1}$.
could occur: $2 p^{3}+2 s^{1}, 2 p^{2}+2 s^{1}$, and $2 p^{1}+2 s^{1}$; this corresponded to single, double, and triple bonds of hybridization of the $\mathrm{sp}^{3}, \mathrm{sp}^{2}$, and sp types.

## Nitrogen $\left(2 s^{2} 2 p^{3}\right)$

$P_{0}$ of the $2 \mathrm{p}^{3}$ orbital was $15.830 \mathrm{eV} \AA$, and $P_{0}$ of the $2 \mathrm{~s}^{1}$ orbital was $10.709 \mathrm{eV} \AA$. Therefore, they were hybridized with the formation of the $2 p_{\Gamma}^{4}$ hybridized orbital responsible for $\sigma$-bond sp hybridization, where $P_{0}$ $=19.193 \mathrm{eV} \AA$. However, this was still greater than $P_{0}$ of the $2 \mathrm{~s}^{2}$ orbitals ( $17.833 \mathrm{eV} \AA$ ). That is, the hybridization process continued due to the $2 s^{2}$ orbital with the formation of the $2 p_{\Gamma}^{5}$ orbital $\left(P_{0}=21.966 \mathrm{eV} \AA\right)$ responsible for the $2 \pi$-bond of $s-p$ hybridization.

There are main hybridization options for orbitals in carbon and nitrogen atoms in this approach. Less possible are metastable states with the hybridization of the $2 s^{2}+2 p^{2}$ type with carbon and the $2 s^{2}+2 p^{3}$ of nitrogen.

The initial hybridization principle was applied to the analysis of the energy directedness of mixing of atom orbitals for some other structures (Table II). The computational values of $P_{0}$ of the hybridized orbitals were further used to determine bond energies $(E)$. In the supposition of pair interatomic interaction, the
structural $P_{C}$ parameter was calculated ${ }^{1,7}$ following the principle of the addition of inverse values of initial values of $P$ and, in this case, based on the following equation:

$$
\begin{equation*}
\frac{1}{E}=\frac{1}{P_{C}}=\frac{1}{\left(P_{E} \frac{N}{\mathbf{K}}\right)_{1}}+\frac{1}{\left(P_{E} \frac{N}{\mathbf{K}}\right)_{2}} \tag{3}
\end{equation*}
$$

where $N$ is the coefficient of the bond repetition factor and K usually equals the number of registered atom valence electrons. The half internuclear distance was frequently used as $R$ for binary bonds. The same was true for the hydrogen atom in halogen-hydrogen.

The corresponding calculations for several structures are given in Table II. As shown in Table II, K in the crystalline carbon structures observed was equal to the coordination number. For the $\sigma$-bond of nitrogen, $K=3$; this corresponded to the number of valence electrons of the $2 p^{3}$ orbital: $K_{1}=n_{1}=3$.

The comparison of computational values with the experimental data by bond energy ${ }^{8}$ given in Table II characterizes rather the high efficiency of this method. Usually, the ratio error does not exceed $0.1 \%$ and is not more than $5 \%$ in other cases.

TABLE IV
$E(\mathrm{~kJ} / \mathrm{mol})$ Values of Bond Breakoff in Complex Structures

| No. | Reaction <br> 1 | Bond breakoff$2$ | First atom |  |  | Second atom |  |  | E |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Orbitals $3$ | $\begin{gathered} N / \kappa \\ 4 \end{gathered}$ | $\begin{gathered} P_{E}(\mathrm{eV}) \\ P_{1} \\ 5 \end{gathered}$ | Orbitals $6$ | $\begin{gathered} N / \kappa \\ 7 \end{gathered}$ | $\begin{gathered} P_{E}(\mathrm{eV}) \\ 8 \end{gathered}$ | $\begin{gathered} \text { Calcd } \\ 9 \end{gathered}$ | Found $10$ |
| 2 | $\begin{aligned} & \mathrm{CH}_{2}=\mathrm{CH}+\mathrm{H} \\ & \mathrm{CH}_{3}=\mathrm{CH}_{2}+\mathrm{H} \end{aligned}$ | $\mathrm{C}-\mathrm{H}$$\mathrm{C}-\mathrm{H}$ | $2 s^{2} 2 p^{2}$ | 1/4 | 7.982 | $1 \mathrm{~s}^{1}$ | 1/1 | 9.0624 | 409.7 | $430 \pm 12.6$ |
|  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & 457 \pm 12.6 \\ & >434.8 \end{aligned}$ |
| 3 | $\mathrm{CH}_{4}=\mathrm{CH}_{3}+\mathrm{H}$ |  |  |  |  |  |  |  |  | $435 \pm 4.2$ |
| 4 | $\mathrm{C}_{2} \mathrm{H}_{4}=\mathrm{C}_{2} \mathrm{H}_{3}+\mathrm{H}$ |  |  |  |  |  |  |  |  | $438.9$ |
| 5 | $\mathrm{C}_{2} \mathrm{H}_{6}=\mathrm{C}_{2} \mathrm{H}_{5}+\mathrm{H}$ |  |  |  |  |  |  | 10.426 | 436.4 | 445.2 |
| 6 | $\mathrm{C}_{6} \mathrm{H}_{6}=\mathrm{C}_{6} \mathrm{H}_{5}+\mathrm{H}$ |  |  |  |  |  |  | 9.0624 | 366.5 | 457.3 |
| 7 | $\mathrm{CH}_{2}=\mathrm{CH}+\mathrm{H}$ |  | $2 \mathrm{p}^{2}$ | 1/2 | 6.533 | $1 \mathrm{~s}^{1}$ | 1/1 |  |  | $338.9$ |
|  |  |  |  |  |  |  |  |  |  | $364$ |
| 8 | $\mathrm{CH}_{4}=\mathrm{CH}_{2}+\mathrm{H}_{2}$ | $\mathrm{C}-\left(\mathrm{H}_{2}\right)$ | $2 \mathrm{p}^{2}$ | 1/2 | 6.533 | $1 \mathrm{~s}^{1}$ | $2 \cdot 1 / 1$ | $2 \cdot 9.0624$ | 463.6 | 432.6 |
| 9 | $\mathrm{C}_{2} \mathrm{H}_{5}=\mathrm{CH}_{3}+\mathrm{CH}_{2}$ | C-C | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{2}$ | 1/4 | 7.982 | $2 s^{2} 2 p^{2}$ | 1/4 | 7.982 | 385.2 | $416.7 \pm 8.4$ |
| 10 | $\mathrm{C}_{2} \mathrm{H}_{6}=2 \mathrm{CH}_{3}$ |  |  |  |  |  |  |  |  | $372.4$ |
| 11 | $\mathrm{C}_{3} \mathrm{H}_{8}=\mathrm{C}_{2} \mathrm{H}_{5}+\mathrm{CH}_{3}$ |  |  |  |  |  |  |  |  | 380.7 |
| 12 | $\mathrm{O}_{2}=\mathrm{O}+\mathrm{O}$ | $\mathrm{O}=\mathrm{O}$ | $2 p^{2}$ | 2/2 | 17.967 | $2 \mathrm{p}^{2}$ | 2/2 | 17.967 |  | - |
| 13 | $\begin{aligned} & \mathrm{CH}_{3} \mathrm{O} \cdot \mathrm{OH}=\mathrm{CH}_{3} \mathrm{O} \\ & +\mathrm{OH} \end{aligned}$ | - $\mathrm{O}-\mathrm{O}-$ | $2 p^{4}$ | 1/4 | $14.954^{\text {a }}$ | $2 \mathrm{p}^{4}$ | 1/4 | $14.954^{\text {a }}$ | 180.4 | $181.5 \pm 19$ |
| 14 | $\mathrm{H}_{2} \mathrm{O}_{2}=2 \mathrm{OH}$ | -O-O- | $2 \mathrm{p}^{2}$ | 1/2 | 8.7192 | $2 \mathrm{p}^{2}$ | 1/2 | 8.7192 | 210.4 | $231.8 \pm 2.5$ |
| 15 | $\mathrm{H}_{2} \mathrm{O}_{2}=2 \mathrm{OH}$ | $(\mathrm{OH})-(\mathrm{OH})$ |  |  | 4.5118 |  |  | 4.5118 | 217.8 | $231.8 \pm 2.5$ |
| 16 | $\mathrm{N}_{2}=2 \mathrm{~N}$ | $\mathrm{N}-\mathrm{N}$ | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{3}$ | $1 / 5$ | 22.745 | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{3}$ | 1/5 | 22.745 | $\begin{aligned} & 219.5 \\ & (2.275 \mathrm{eV}) \end{aligned}$ |  |
| 17 | $\mathrm{N}_{2} \mathrm{H}_{2}=\mathrm{NH}+\mathrm{NH}$ | $\mathrm{N}=\mathrm{N}$ | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{3}$ | $2 / 5$ | $22.745 \frac{2}{5}$ | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{3}$ | 2/5 | $8.898^{\text {a }}$ | 439.1 | $472.8 \pm 33.5$ |
|  |  |  |  | 2/3 | $=8.898^{a}$ | $1 \mathrm{~s}^{1}$ | 1/1 |  |  |  |
| 18 |  | $\mathrm{N}=\mathrm{N}$ | $2 p^{3}$ |  | $10.696^{\text {a }}$ |  |  | $9.0624$ | $\left(P_{\mathrm{i}}=5.118 \mathrm{eV}\right)$247 |  |
| 19 | $\mathrm{N}_{2} \mathrm{H}_{4}=2\left(\mathrm{NH}_{2}\right)$ | $\left(\mathrm{NH}_{2}\right)-\left(\mathrm{NH}_{2}\right)$ |  |  | $5.118^{\text {a }}$ |  |  | $5.118^{\text {a }}$ |  | $252.7 \pm 16.7$ |
| 20 | $\begin{aligned} & \mathrm{CH}_{3} \mathrm{NHNH}_{2}=\mathrm{CH}_{3} \mathrm{NH} \\ & +\mathrm{NH}_{2} \end{aligned}$ | $\mathrm{N}-\mathrm{N}$ | $2 \mathrm{p}^{3}$ | 1/3 | $10.696^{\text {a }}$ | $2 \mathrm{P}^{3}$ | 1/3 | $10.696^{\text {a }}$ | 172.1 | 175.7 |
|  |  | $\mathrm{N}-\mathrm{N}$ | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{3}$ | $1 / 5$ | $22.745^{\text {a }}$ | $2 S^{2} 2 \mathrm{P}^{3}$ | 1/5 | $22.745^{\text {a }}$ | 219.5 | $217 \pm 4$ |
| 21 | $\mathrm{NO}_{2}=\mathrm{NO}+\mathrm{O}$ | $(\equiv \mathrm{N}=\mathrm{O})-\mathrm{O}$ | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{3}$ | - | 4.4525 | $2 \mathrm{P}^{2}$ | 2/2 | $8.7191^{\text {a }}$ | 284.5 | 305.9 |
| 22 | $\mathrm{N}_{2} \mathrm{O}=\mathrm{NO}+\mathrm{N}$ | $\mathrm{N}-\mathrm{O}$ | $2 \mathrm{p}^{1}$ | 1/1 | 9.2839 | $2 \mathrm{P}^{1}$ | 1/1 | 9.7979 | 460.2 | 481.8 |
| 23 | $\mathrm{N}_{2} \mathrm{O}=\left(\mathrm{N}_{2}\right)+\mathrm{O}$ | $\left(\mathrm{N}_{2}\right)=\mathrm{O}$ | - | - | $22.745^{\text {a }}$ | - | - | $8.7191^{\text {a }}$ | 172.5 | 167.4 |
| 24 | $\mathrm{NO}_{2}=\mathrm{N}+\mathrm{O}_{2}$ | $(\mathrm{N})-\left(\mathrm{O}_{2}\right)$ | $2 \mathrm{~s}^{2} 2 \mathrm{p}^{2}$ | 1/5 | 9.4826 | - | - | 8.9835 | 445.3 | 439.3 |

${ }^{\text {a }}$ Calculations of $P_{E}$ were done with $r_{1}$.

Also, the given model mainly confirmed the approved conclusions and results of the corresponding computational methods of bond energies as applicable to certain structures, the list of which in this article is limited only by the authors' interests.

## Calculation of chemical bond energy via the average values of $p_{0}$

The application of methods of valence bonding and molecular orbitals to complex structures meets significant difficulties with regard to the prediction of hybridization energy directedness and the type of bonds being formed. Let us consider several opportunities of with $P_{0}$ method. It is practical to apply eq. (3) to calculate the energy of chemical bonds, where K usually equals the number of registered valence electrons and $P_{E}(N / K)$ has a physical sense of the averaged energy of the spatial energy parameter falling on one valence electron of registered orbitals. However, for complex structures, $P(\mathrm{~N} / \mathrm{K})$ is averaged by all of the main valence orbitals.
Let us first approve such an approach for binary molecules. For binary molecules, the dissociation en-
ergy $\left(D_{0}\right)$ corresponds to the value of chemical bond energy: $D_{0}=E$.

The results of the calculation of $D_{0}$ by eq. (3) given in Table III showed that $P_{C}=D_{0}$. For some molecules containing $\mathrm{F}, \mathrm{N}$, and O , the values of $r_{I}$ (in Table III marked with a superscript $a$ ) were used to register the ionic character of the bond in the process of $P_{E}$ calculation. For molecules $\mathrm{C}_{2}, \mathrm{~N}_{2}$, and $\mathrm{O}_{2}$, the calculations were done by divisible bonds. In other cases, the average values of bond energy were calculated. The computational data were not in conflict with the experimental data. ${ }^{8}$

With a similar computation of average values of bond energy in complex structures, the average values of $P_{E}$ (taken from Table I) were also considered but with valence sublevels taken into account (Table IV). In these cases, $P_{C}=E$ (bond energy).

Also, in most cases, due to the influence of all of the valence electrons of atoms, it was possible for the first approximation to be limited with the estimation of interaction only between basic bond atoms (e.g., $\mathrm{C}-\mathrm{H}$ in hydrocarbon structures). To a greater extent, this
refers to hydrocarbon organic structures. However, for nitrogen oxides and hydrides, more accurate results were obtained with preliminary calculations of the $P_{C}$ values of the reaction intermediate products with eq. (3).

Then, $E$ was calculated according to the following equation:

$$
\begin{equation*}
\frac{1}{E}=\frac{1}{P_{C 1}}+\frac{1}{P_{C 2}} \tag{4}
\end{equation*}
$$

where $P_{C 1}$ and $P_{C 2}$ are the $P_{C}$ values of complex structure parameters.

Calculations based on eqs. (3) and (4) are given in Tables III and IV. In some cases, the results of the calculations of bond energy for fragments of $\mathrm{NH}_{2}$, $\mathrm{NO}_{2}$, and $\mathrm{N}_{2} \mathrm{O}$ that were introduced into other complex structures are given. The deviations of the computational data from the experimental ones ${ }^{8}$ did not exceed $10 \%$ for complex structures.

## CONCLUSIONS

1. The energy of chemical bonds in simple and complex structures could be satisfactorily deter-
mined by means of the $P$ method on the basis of the initial spatial energy characteristics of free atoms with the hybridization of their atom orbitals taken into account.
2. The proposed method for the estimation of the energy directedness of mixing atom orbitals agreed with the experimental data.

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